

Student Workbook

Law of Sines

Name: _____

Date: _____

Period: _____

Learning Target: I can use the Law of Sines to solve oblique triangles, including the ambiguous (SSA) case, and find their area.

Vocabulary

Term	Meaning
Oblique Triangle	A triangle that does NOT contain a right angle.
Law of Sines	$a/\sin A = b/\sin B = c/\sin C$ — relates each side to the sine of its OPPOSITE angle.
Ambiguous Case (SSA)	Given two sides and a non-included angle, there may be 0, 1, or 2 valid triangles.

Key Concept: Solving AAS/ASA Triangles

METHOD 1. Find the third angle (angles sum to 180°). 2. Use the Law of Sines to solve for each missing side.

EXAMPLE 1
Triangle with $A=40^\circ$, $B=60^\circ$, $a=10$. Find b and c .

$C = 180^\circ - 40^\circ - 60^\circ = \underline{\hspace{2cm}}$
 $b = 10\sin(60^\circ)/\sin(40^\circ) \approx \underline{\hspace{2cm}}$ $c = 10\sin(80^\circ)/\sin(40^\circ) \approx \underline{\hspace{2cm}}$

Key Concept: The Ambiguous Case (SSA)

WHY IT'S TRICKY When given two sides and a non-included angle, solving for the other angle using arcsin can give TWO possible angles (θ and $180^\circ-\theta$). You must check whether each leads to a valid triangle (angle sum $< 180^\circ$).

EXAMPLE 2

$A=30^\circ$, $a=5$, $b=8$. How many triangles are possible?

$$\sin B = 8\sin(30^\circ)/5 = \underline{\hspace{2cm}} \rightarrow B \approx \underline{\hspace{2cm}}^\circ \text{ or } \underline{\hspace{2cm}}^\circ$$

Check both: both give a valid third angle $C > 0^\circ$, so there are $\underline{\hspace{2cm}}$ solutions.

COMMON MISTAKE

Always check BOTH possible angles from arcsin in an SSA problem! Forgetting the second angle ($180^\circ - \theta$) is the most common error — and sometimes that second triangle is invalid, which is just as important to notice.

Key Concept: Area of an Oblique Triangle

FORMULA Area = $\frac{1}{2}ab \cdot \sin C$ (using two sides and their INCLUDED angle)

EXAMPLE 3

Find the area of a triangle with $a=7$, $b=9$, $C=50^\circ$.

$$\text{Area} = \frac{1}{2}(7)(9)\sin(50^\circ) \approx \underline{\hspace{2cm}}$$

Guided Practice — Part A: Solve the Triangle (Two Angles + Side)

A1 $A=50^\circ$, $B=70^\circ$, $a=8$. Find b and c .

A2 $A=35^\circ$, $C=95^\circ$, $c=20$. Find a and b .

Guided Practice — Part B: Solve the Triangle (Included Side)

B1 $A=45^\circ$, $C=65^\circ$, $b=10$. Find a and c .

B2 $A=55^\circ$, $B=60^\circ$, $c=14$. Find a and b .

Guided Practice — Part C: The Ambiguous Case

C1 $A=30^\circ$, $a=5$, $b=8$. How many solutions are there?

C2 $A=50^\circ$, $a=10$, $b=6$. How many solutions are there?

Guided Practice — Part D: Area of a Triangle

D1 $a=6$, $b=10$, $C=40^\circ$. Find the area.

D2 $a=9$, $b=12$, $C=65^\circ$. Find the area.

BEFORE YOU MOVE ON

Check with a partner: for SSA problems, did you check whether BOTH possible angles actually produce a valid triangle?